

Name: \_\_\_\_\_

Class: \_\_\_\_\_

### Linear / Exponential Functions Day One: Word Problems

#### Question 1

The population of bacteria in a laboratory is modeled by the function  $f(x) = 900 * 3^x$  where  $x$  represents weeks.

- a. Explain what the 900 represents in the context of the problem
  
  
  
  
  
  
  
  
  
  
- b. Explain what the 3 represents in the context of the problem
  
  
  
  
  
  
  
  
  
  
- c. Find the population of bacteria after 3 months

#### Question 2

A taxicab charges a flat rate of \$3.50 for the first 4 miles plus \$1.50 for each additional mile driven.

- a. Create a linear function,  $C(m)$ , of this situation.
  
  
  
  
  
  
  
  
  
  
- b. If the cab has driven 17 miles, find how much the ride costs. Show your work.
  
  
  
  
  
  
  
  
  
  
- c. If Todd pays \$26 for the ride, how many miles did the cab driver take Todd? Show your work.

#### Question 3 (Linear Inequality Review)

If  $a = 3$ , find the largest integer for  $x$  that will satisfy the inequality below:

$$ax + x(2a - 4) < x + 24$$

(a) 2

(b) 3

(c) 4

(d) 5

Question 4

Donald Duck painted his house white. Below is the surface area of the house that was painted white based on hours.

Hours	1	2	3	4
Surface Area Painted White ( $ft^2$ )	38	62	86	110

Donald wrote an equation for the surface area of the house painted white,  $y$ , based on  $x$  hours. He believes the  $y$ -intercept is equal to  $38 ft^2$ . Choose the correct statement.

- (1) Donald is correct because 38 is the number that first appears in the table.
- (2) Donald is correct because the  $y$ -intercept is the value of  $y$  when  $x$  is equal to 1.
- (3) Donald is incorrect because the  $y$ -intercept is the value of  $y$  when  $x$  is equal to 0.
- (4) Donald is incorrect because the value of  $y$  increases by 24 every time the value of  $x$  increases by 1.

Question 5-8

5.

The growth of a certain organism can be modeled by  $C(t) = 10(1.029)^{24t}$ , where  $C(t)$  is the total number of cells after  $t$  hours. Which function is approximately equivalent to  $C(t)$ ?

- 1)  $C(t) = 240(.083)^{24t}$
- 2)  $C(t) = 10(.083)^t$
- 3)  $C(t) = 10(1.986)^t$
- 4)  $C(t) = 240(1.986)^{\frac{t}{24}}$

7.

Mario's \$15,000 car depreciates in value at a rate of 19% per year. The value,  $V$ , after  $t$  years can be modeled by the function  $V = 15,000(0.81)^t$ . Which function is equivalent to the original function?

- 1)  $V = 15,000(0.9)^{9t}$
- 2)  $V = 15,000(0.9)^{2t}$
- 3)  $V = 15,000(0.9)^{\frac{t}{9}}$
- 4)  $V = 15,000(0.9)^{\frac{t}{2}}$

6.

Materials  $A$  and  $B$  decay over time. The function for the amount of material  $A$  is  $A(t) = 1000(0.5)^{2t}$  and for the amount of material  $B$  is  $B(t) = 1000(0.25)^t$ , where  $t$  represents time in days. On which day will the amounts of material be equal?

- 1) initial day, only
- 2) day 2, only
- 3) day 5, only
- 4) every day

8.

Sheba opened a retirement account with \$36,500. Her account grew at a rate of 7% per year compounded annually. She made no deposits or withdrawals on the account. At the end of 20 years, what was the account worth, to the nearest dollar?

- 1) \$87,600
- 2) \$130,786
- 3) \$141,243
- 4) \$1,483,444,463

Question 9

Marilyn collects old dolls. She purchases a doll for \$450. Research shows this doll's value will increase by 2.5% each year. Write an equation that determines the value,  $V$ , of the doll  $t$  years after purchase. Assuming the doll's rate of appreciation remains the same, will the doll's value be doubled in 20 years? Justify your reasoning.

Question 10

A car was purchased for \$25,000. Research shows that the car has an average yearly depreciation rate of 18.5%.

Create a function that will determine the value,  $V(t)$ , of the car  $t$  years after purchase.

Determine, to the *nearest cent*, how much the car will depreciate from year 3 to year 4.

Questions 11-14

<p>11.</p> <p>A company that manufactures radios first pays a start-up cost, and then spends a certain amount of money to manufacture each radio. If the cost of manufacturing <math>r</math> radios is given by the function <math>c(r) = 5.25r + 125</math>, then the value 5.25 best represents</p> <ol style="list-style-type: none"><li>1) the start-up cost</li><li>2) the profit earned from the sale of one radio</li><li>3) the amount spent to manufacture each radio</li><li>4) the average number of radios manufactured</li></ol>	<p>12.</p> <p>The amount Mike gets paid weekly can be represented by the expression <math>2.50a + 290</math>, where <math>a</math> is the number of cell phone accessories he sells that week. What is the constant term in this expression and what does it represent?</p> <ol style="list-style-type: none"><li>1) <math>2.50a</math>, the amount he is guaranteed to be paid each week</li><li>2) <math>2.50a</math>, the amount he earns when he sells <math>a</math> accessories</li><li>3) 290, the amount he is guaranteed to be paid each week</li><li>4) 290, the amount he earns when he sells <math>a</math> accessories</li></ol>
<p>13.</p> <p>The cost of airing a commercial on television is modeled by the function <math>C(n) = 110n + 900</math>, where <math>n</math> is the number of times the commercial is aired. Based on this model, which statement is true?</p> <ol style="list-style-type: none"><li>1) The commercial costs \$0 to produce and \$110 per airing up to \$900.</li><li>2) The commercial costs \$110 to produce and \$900 each time it is aired.</li><li>3) The commercial costs \$900 to produce and \$110 each time it is aired.</li><li>4) The commercial costs \$1010 to produce and can air an unlimited number of times.</li></ol>	<p>14.</p> <p>Each day, a local dog shelter spends an average of \$2.40 on food per dog. The manager estimates the shelter's daily expenses, assuming there is at least one dog in the shelter, using the function <math>E(x) = 30 + 2.40x</math>.</p> <p>Which statements regarding the function <math>E(x)</math> are correct?</p> <p>I. <math>x</math> represents the number of dogs at the shelter per day. II. <math>x</math> represents the number of volunteers at the shelter per day. III. 30 represents the shelter's total expenses per day. IV. 30 represents the shelter's nonfood expenses per day.</p> <ol style="list-style-type: none"><li>(1) I and III</li><li>(2) I and IV</li><li>(3) II and III</li><li>(4) II and IV</li></ol>

Question 15

During physical education class, Andrew recorded the exercise times in minutes and heart rates in beats per minute (bpm) of four of his classmates. Which table best represents a linear model of exercise time and heart rate?

**Student 1**

<b>Exercise Time</b> (in minutes)	<b>Heart Rate</b> (bpm)
0	60
1	65
2	70
3	75
4	80

(1)

**Student 3**

<b>Exercise Time</b> (in minutes)	<b>Heart Rate</b> (bpm)
0	58
1	65
2	70
3	75
4	79

(3)

**Student 2**

<b>Exercise Time</b> (in minutes)	<b>Heart Rate</b> (bpm)
0	62
1	70
2	83
3	88
4	90

(2)

**Student 4**

<b>Exercise Time</b> (in minutes)	<b>Heart Rate</b> (bpm)
0	62
1	65
2	66
3	73
4	75

(4)

Question 16

Which of the three situations given below is best modeled by an exponential function?

- I. A bacteria culture doubles in size every day.
- II. A plant grows by 1 inch every 4 days.
- III. The population of a town declines by 5% every 3 years.

- (1) I, only
- (2) II, only
- (3) I and II
- (4) I and III